

Test y and z by investigating their behavior at (i) $x_1 = 0$ (ii) $x_1 = x_0$; and what happens as (iii) $x_0 \rightarrow \infty$.

(i) If $x_1 = 0$ then ~~excepted~~ this will force the point P_1 to be ~~at~~ the point P . $\boxed{P_1 = P}$

$$y = \frac{-y_1 x_0}{x_1 - x_0} ; \quad z = \frac{-z_1 x_0}{x_1 - x_0}$$

$$y = \frac{-y_1 x_0}{0 - x_0}$$

$$y = \frac{y_1(-x_0)}{(-x_0)}$$

$$\boxed{y = y_1}$$

$$z = \frac{z_1(-x_0)}{0 - x_0}$$

$$\boxed{z = z_1}$$

(ii) If $x_1 = x_0$ then the vector will never pass through the yz -plane and y and z will be undefined. *Good!*

$$y = \frac{-y_1 x_0}{x_1 - x_0}$$

z is same as y

$$y = \frac{-y_1 x_1}{x_1 - x_1} \quad | x_1 = x_0 \leftarrow$$

$$\boxed{y = \frac{-y_1 x_1}{0} \text{ undefined}}$$

(iii) ~~As $x_0 \rightarrow \infty$ both y and z approach 1, meeting the point (approach $(0, 1, 1)$)~~

(Sorry)

~~As $x_0 \rightarrow \infty$ both y and z approach y_1 or z_1 , until they actually reached infinity respectively.~~

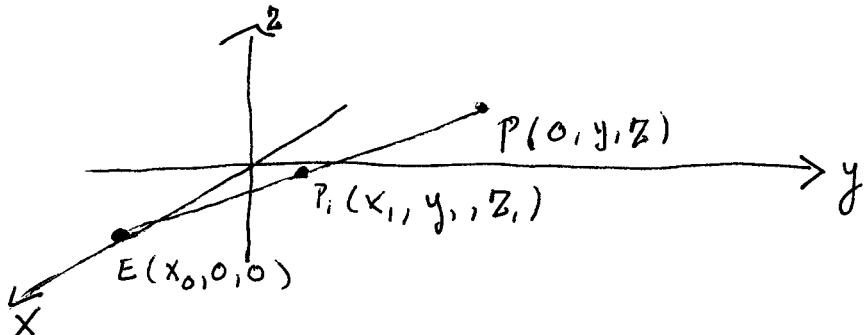
This happens because the amount x_1 is subtracting becomes null unless $x_1 \rightarrow \infty$. Otherwise the two will be close enough to make $\frac{x_1}{x_0} \rightarrow 1$ marking $y \rightarrow y_1$.

Excellent job.

For the following problem I worked so with only the aid of our text and my notes.

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Q) The Eye is at $E(x_0, 0, 0)$. We want to portray the point $P_1(x_1, y_1, z_1)$ on the yz -plane, this point will be $P(0, y, z)$. The problem is to find y and z given E and P_1 .



a) Write a vector equation that holds true between \vec{EP} and \vec{EP}_1 . Use the equation to express y and z in terms of x_0, x_1, y_1, z_1 :

$$\vec{EP} = \vec{EP}_1 + \vec{P_1P}$$

Now since we are trying to \vec{EP} that passes through the point P_1 a restriction is that $x_0 > x_1$, otherwise the vector will never pass through the yz -plane. Thus the point P can be defined through the parametric equation of \vec{EP}_1 by defining t through the fact that x must always equal zero.

$$\vec{EP}_1 = \langle x_1 - x_0, y_1 - 0, z_1 - 0 \rangle$$

$E(x_0, 0, 0)$

$$(x, y, z) = (x_0 + (x_1 - x_0)t, y_1 t, z_1 t)$$

$$x = 0 = x_0 + (x_1 - x_0)t$$

$$-x_0 = (x_1 - x_0)t$$

$$t = \frac{-x_0}{x_1 - x_0} \quad (\text{Good!})$$

$$P(0, y, z) = \left(0, \frac{-y_1 x_0}{x_1 - x_0}, \frac{-z_1 x_0}{x_1 - x_0}\right)$$

$$y = \frac{-y_1 x_0}{x_1 - x_0} \quad ; \quad z = \frac{-z_1 x_0}{x_1 - x_0}$$

if $x_0 > x_1$ and $x = 0$